

## Kohn-Sham DFT

$$\left[ -\frac{\nabla^2}{2} + v_{ext} + V^{\mathcal{H}c} \right] \phi_p^{\mathcal{KS}} = \varepsilon_p^{\mathcal{KS}} \phi_p^{\mathcal{KS}}$$

Fundamental gap

## GW approximation

$$\varepsilon_p^{GW} = \varepsilon_p^{\mathcal{KS}} + \langle \phi_p^{\mathcal{KS}} | \Sigma^{GW}(\varepsilon_p^{GW}) - V^{\mathfrak{C}} | \phi_p^{\mathcal{KS}} \rangle$$

Ionization potentials  
Electron affinities

## (Inverse) photoemission spectroscopy

Excitonic effect

## Bethe-Salpeter equation

$$\begin{pmatrix} R & C \\ -C^* & -R^* \end{pmatrix} \begin{pmatrix} X_m \\ Y_m \end{pmatrix} = \Omega_m \begin{pmatrix} X_m \\ Y_m \end{pmatrix}$$

Optical excitations

## Optical spectroscopy